## FINAL NEET(UG)-2021 EXAMINATION

## (Held On Sunday 12 ${ }^{\text {th }}$ SEPTEMBER, 2021)

## PHYSICS

## SECTION - A (PHYSICS)

1. An inductor of inductance $L$, a capacitor of capacitance C and a resistor of resistance ' R ' are connected in series to an ac source of potential difference ' V ' volts as shown in figure.

Potential difference across $\mathrm{L}, \mathrm{C}$ and R is 40 V , 10 V and 40 V , respectively. The amplitude of current flowing through LCR series circuit is $10 \sqrt{2} \mathrm{~A}$. The impedance of the circuit is :-

(1) $4 \sqrt{2} \Omega$
(2) $5 / \sqrt{2} \Omega$
(3) $4 \Omega$
(4) $5 \Omega$

Ans. (4)
Sol. $I_{0}=10 \sqrt{2} \mathrm{~A}$
$\mathrm{I}_{\mathrm{RMS}}=\frac{\mathrm{I}_{0}}{\sqrt{2}}=10 \mathrm{~A}$

$\mathrm{V}_{\mathrm{RMS}}=\sqrt{\mathrm{V}_{\mathrm{R}}^{2}+\left(\mathrm{V}_{\mathrm{L}}-\mathrm{V}_{\mathrm{C}}\right)^{2}}$
$=\sqrt{(40)^{2}+(40-10)^{2}}$
$=50 \mathrm{~V}$
$\mathrm{Z}=\frac{\mathrm{V}_{\text {RMS }}}{\mathrm{I}_{\text {RMS }}}=\frac{50 \mathrm{~V}}{10 \mathrm{~V}}=5 \Omega$

## TEST PAPER WITH ANSWER \& SOLUTION

For Hindi :-
$\mathrm{I}_{\mathrm{rms}}=10 \sqrt{2} \mathrm{~A}$


$$
\begin{aligned}
\mathrm{V}_{\mathrm{rms}} & =\sqrt{\mathrm{V}_{\mathrm{R}}^{2}+\left(\mathrm{V}_{\mathrm{L}}-\mathrm{V}_{\mathrm{C}}\right)^{2}} \\
& =\sqrt{40^{2}+(40-10)^{2}} \\
& =50 \mathrm{~V} \\
\mathrm{Z} & =\frac{\mathrm{V}_{\mathrm{rms}}}{\mathrm{I}_{\mathrm{rms}}}=\frac{50 \mathrm{~V}}{10 \sqrt{2} \mathrm{~A}}=\frac{5}{\sqrt{2}} \Omega
\end{aligned}
$$

2. Find the value of the angle of emergence from the prism. Refractive index of the glass is $\sqrt{3}$.

(1) $60^{\circ}$
(2) $30^{\circ}$
(3) $45^{\circ}$
(4) $90^{\circ}$

Ans. (1)

Sol.

$r_{1}+r_{2}=A=30^{\circ}$
$r_{2}=30^{\circ}\left(r_{1}=0^{\circ}\right)$
from Snell's law
$\sqrt{3} \sin r_{2}=1 \times \sin e$
$\sqrt{3} \sin 30^{\circ}=$ sine
$e=60^{\circ}$
3. A dipole is placed in an electric field as shown. In which direction will it move ?

(1) towards the left as its potential energy will increase.
(2) towards the right as its potential energy will decrease.
(3) towards the left as its potential energy will decrease.
(4) towards the right as its potential energy will increase.
Ans. (2)
Sol. $\left|\overrightarrow{\mathrm{E}}_{1}\right|>\left|\overrightarrow{\mathrm{E}}_{2}\right|$
as field lines are closer at charge +q , so net force on the dipole acts towards right side. A system always moves to decrease it's potential energy.

4. A capacitor of capacitance ' $C$ ', is connected across an ac source of voltage V , given by $\mathrm{V}=\mathrm{V}_{0} \sin \omega \mathrm{t}$
The displacement current between the plates of the capacitor, would then be given by :
(1) $I_{d}=V_{0} \omega C \cos \omega t$
(2) $I_{d}=\frac{V_{0}}{\omega C} \cos \omega t$
(3) $I_{d}=\frac{V_{0}}{\omega C} \sin \omega t$
(4) $I_{d}=V_{0} \omega C \sin \omega t$

Ans. (1)
Sol. $q=C V$

$$
\frac{\mathrm{dq}}{\mathrm{dt}}=\frac{\mathrm{CdV}}{\mathrm{dt}}
$$

$$
\begin{aligned}
\mathrm{I}_{\mathrm{d}} & =\mathrm{C}\left(\mathrm{~V}_{0} \omega \cos \omega \mathrm{t}\right) \\
& =\mathrm{V}_{0} \omega \mathrm{C} \cos \omega \mathrm{t}
\end{aligned}
$$

5. A thick current carrying cable of radius 'R' carries current 'I' uniformly distributed across its cross-section. The variation of magnetic field $\mathrm{B}(\mathrm{r})$ due to the cable with the distance 'r' from the axis of the cable is represented by :
(1)

(2)

(3)

(4)


Ans. (3)
Sol. Inside a current carrying cylindrical conductor,

$$
B=\frac{\mu_{0} I}{2 \pi R^{2}} r \quad \therefore B \propto r
$$

Outside the conductor,

$$
\mathrm{B}=\frac{\mu_{0} \mathrm{I}}{2 \pi \mathrm{r}} \therefore \mathrm{~B} \propto \frac{1}{\mathrm{r}}
$$


6. A convex lens ' A ' of focal length 20 cm and a concave lens ' B ' of focal length 5 cm are kept along the same axis with a distance 'd' between them. If a parallel beam of light falling on 'A' leaves 'B' as a parallel beam, then the distance 'd' in cm will be :-
(1) 25
(2) 15
(3) 50
(4) 30

Ans. (2)

Sol.

$\mathrm{d}=\mathrm{f}_{1}-\mathrm{f}_{2}$
$=20-5$
$=15 \mathrm{~cm}$
7. An electromagnetic wave of wavelength ' $\lambda$ ' is incident on a photosensitive surface of negligible work function. If ' $m$ ' mass is of photoelectron emitted from the surface has de-Broglie wavelength $\lambda_{\mathrm{d}}$, then :
(1) $\lambda=\left(\frac{2 m}{h c}\right) \lambda_{d}^{2}$
(2) $\lambda_{d}=\left(\frac{2 m c}{h}\right) \lambda^{2}$
(3) $\lambda=\left(\frac{2 m c}{h}\right) \lambda_{d}^{2}$
(4) $\lambda=\left(\frac{2 h}{m c}\right) \lambda_{d}^{2}$

Ans. (3)
Sol. $\frac{\mathrm{hc}}{\lambda}=\mathrm{K}_{\max }+\phi \quad$ [given $\phi$ is neglibible]
so, $\frac{\mathrm{hc}}{\lambda}=\mathrm{K}_{\max }$
$\lambda_{\mathrm{d}}=\frac{\mathrm{h}}{\sqrt{2 \mathrm{~m} \mathrm{~K}_{\max }}} \Rightarrow \mathrm{K}_{\max }=\frac{\mathrm{h}^{2}}{2 \mathrm{~m} \lambda_{\mathrm{d}}^{2}}$
$\left(\frac{\mathrm{hc}}{\lambda}\right)=\frac{\mathrm{h}^{2}}{2 \mathrm{~m} \lambda_{\mathrm{d}}^{2}} \Rightarrow \lambda=\left(\frac{2 \mathrm{mc}}{\mathrm{h}}\right) \lambda_{\mathrm{d}}^{2}$
8. Column-I gives certain physical terms associated with flow of current through a metallic conductor. Column-II gives some mathematical relations involving electrical quantities. Match Column-I and Column-II with appropriate relations.

| Column-I |  | Column-II |  |
| :--- | :--- | :--- | :--- |
| (A) | Drift <br> Velocity | (P) | $\frac{\mathrm{m}}{n e^{2} \rho}$ |
| (B) | Electrical <br> Resistivity | (Q) | $n v_{\mathrm{d}}$ |
| (C) | Relaxation <br> Period | (R) | $\frac{\mathrm{eE}}{\mathrm{m}} \tau$ |
| (D) | Current <br> Density | (S) | $\frac{\mathrm{E}}{\mathrm{J}}$ |

(1) (A)-(R), (B)-(S), (C)-(P), (D)-(Q)
(2) (A)-(R), (B)-(S), (C)-(Q), (D)-(P)
(3) (A)-(R), (B)-(P), (C)-(S), (D)-(Q)
(4) (A)-(R), (B)-(Q), (C)-(S), (D)-(P)

Ans. (1)
Sol. (A) $v_{d}=\left(\frac{e E}{m}\right) \tau$
(B) $\mathrm{J}=\sigma \mathrm{E}=\mathrm{E} / \rho$ $\Rightarrow \rho=\mathrm{E} / \mathrm{J}$
(C) $\rho=\frac{E}{n e v_{d}}$

$$
\begin{gathered}
v_{d}=\frac{E}{n e \rho} \\
\frac{e E}{m} \tau=\frac{E}{n e \rho} \\
\tau=\frac{m}{n e^{2} \rho} \\
\text { (D) } i=n e A v_{d} \\
\frac{i}{A}=n e v_{d} \\
J=n e v_{d}
\end{gathered}
$$

9. A radioactive nucleus ${ }_{Z}^{A} \mathrm{X}$ undergoes spontaneous decay in the sequence
${ }_{\mathrm{Z}}^{\mathrm{A}} \mathrm{X} \rightarrow{ }_{\mathrm{Z-1}} \mathrm{~B} \rightarrow{ }_{\mathrm{Z}-3} \mathrm{C} \rightarrow{ }_{\mathrm{Z-2}} \mathrm{D}$, where Z is the atomic number of element X . The possible decay particles in the sequence are :
(1) $\alpha, \beta^{-}, \beta^{+}$
(2) $\alpha, \beta^{+}, \beta^{-}$
(3) $\beta^{+}, \alpha, \beta^{-}$
(4) $\beta^{-}, \alpha, \beta^{+}$

Ans. (3)
Sol. $\quad{ }_{Z}^{A} X \xrightarrow{B^{+}}{ }_{Z-1} B \xrightarrow{\alpha}{ }_{Z-3} C \xrightarrow{\beta^{-}}{ }_{Z-2} D$
$\beta^{+}$decreases atomic number by 1
$\alpha$ decreases atomic number by 2
$\beta^{-}$increases atomic number by 1
10. The effective resistance of a parallel connection that consists of four wires of equal length, equal area of cross-section and same material is $0.25 \Omega$. What will be the effective resistance if they are connected in series?
(1) $0.25 \Omega$
(2) $0.5 \Omega$
(3) $1 \Omega$
(4) $4 \Omega$

Ans. (4)
Sol. $R_{\|}=\frac{R}{4}=0.25 \Omega$


$$
\begin{aligned}
& \mathrm{R}=1 \Omega \\
& \begin{aligned}
\mathrm{R}_{\text {series }} & =4 \mathrm{R} \\
& =4(1) \\
& =4 \Omega
\end{aligned}
\end{aligned}
$$

11. A particle is released from height $S$ from the surface of the Earth. At a certain height its kinetic energy is three times its potential energy. The height from the surface of earth and the speed of the particle at that instant are respectively :
(1) $\frac{\mathrm{S}}{4}, \frac{3 \mathrm{gS}}{2}$
(2) $\frac{\mathrm{S}}{4}, \frac{\sqrt{3 \mathrm{gS}}}{2}$
(3) $\frac{\mathrm{S}}{2}, \frac{\sqrt{3 \mathrm{gS}}}{2}$
(4) $\frac{S}{4}, \sqrt{\frac{3 g S}{2}}$

Ans. (4)
Sol. $U+K E=E$
$4 \mathrm{U}=\mathrm{E}=\mathrm{mgS}$
$4 \mathrm{mgh}=\mathrm{mgS}$
$h=\frac{S}{4}$
$\mathrm{V}=\sqrt{2 \mathrm{~g}\left(\frac{3 \mathrm{~S}}{4}\right)}=\sqrt{\frac{3 \mathrm{gS}}{2}}$
12. The half-life of a radioactive nuclide is 100 hours. The fraction of original activity that will remain after 150 hours would be :
(1) $1 / 2$
(2) $\frac{1}{2 \sqrt{2}}$
(3) $\frac{2}{3}$
(4) $\frac{2}{3 \sqrt{2}}$

Ans. (2)
Sol. $\frac{\mathrm{A}}{\mathrm{A}_{0}}=\left(\frac{1}{2}\right)^{\mathrm{t} / \mathrm{T}_{\mathrm{H}}}=\left(\frac{1}{2}\right)^{150 / 100}=\frac{1}{2 \sqrt{2}}$
13. A cup of coffee cools from $90^{\circ} \mathrm{C}$ to $80^{\circ} \mathrm{C}$ in $t$ minutes, when the room temperature is $20^{\circ} \mathrm{C}$. The time taken by a similar cup of coffee to cool from $80^{\circ} \mathrm{C}$ to $60^{\circ} \mathrm{C}$ at a room temperature same at $20^{\circ} \mathrm{C}$ is :
(1) $\frac{13}{10} \mathrm{t}$
(2) $\frac{13}{5} \mathrm{t}$
(3) $\frac{10}{13} \mathrm{t}$
(4) $\frac{5}{13} \mathrm{t}$

Ans. (2)
Sol. According to Newton's law of cooling

$$
\frac{\mathrm{T}_{1}-\mathrm{T}_{2}}{\mathrm{t}}=\mathrm{K}\left[\frac{\mathrm{~T}_{1}+\mathrm{T}_{2}}{2}-\mathrm{T}_{0}\right]
$$

For $1^{\text {st }}$ cup of coffee,
$\Rightarrow \quad \frac{90-80}{\mathrm{t}}=\mathrm{K}\left[\frac{90+80}{2}-20\right]$

For $2^{\text {nd }}$ cup of coffee,
$\Rightarrow \quad \frac{80-60}{\mathrm{t}^{\prime}}=\mathrm{K}\left[\frac{80+60}{2}-20\right]$
Divide (1) by (2)
$\frac{t^{\prime}}{2 \mathrm{t}}=\frac{65}{50} \Rightarrow \mathrm{t}^{\prime}=\frac{13}{5} \mathrm{t}$
14. The number of photons per second on an average emitted by the source of monochromatic light of wavelength 600 nm , when it delivers the power of $3.3 \times 10^{-3}$ watt will be : $\left(\mathrm{h}=6.6 \times 10^{-34} \mathrm{Js}\right)$
(1) $10^{18}$
(2) $10^{17}$
(3) $10^{16}$
(4) $10^{15}$

Ans. (3)
Sol. $\mathrm{p}=\frac{\mathrm{nhc}}{\lambda} \Rightarrow \mathrm{n}=\frac{\mathrm{p} \lambda}{\mathrm{hc}}$
$\mathrm{n}=\frac{3.3 \times 10^{-3} \times 600 \times 10^{-9}}{6.6 \times 10^{-34} \times 3 \times 10^{8}} \simeq 10^{16}$
15. A body is executing simple harmonic motion with frequency ' $n$ ', the frequency of its potential energy is :-
(1) $n$
(2) $2 n$
(3) $3 n$
(4) $4 n$

## Ans. (2)

Sol. Displacement equation of SHM of frequency ' $n$ '
$x=A \sin (\omega t)=A \sin (2 \pi n t)$
Now,

Potential energy $U=\frac{1}{2} k x^{2}=\frac{1}{2} K A^{2} \sin ^{2}(2 \pi n t)$

$$
=\frac{1}{2} \mathrm{kA}^{2}\left[\frac{1-\cos (2 \pi(2 \mathrm{n}) \mathrm{t})}{2}\right]
$$

So frequency of potential energy $=2 n$
16. An infinitely long straight conductor carries a current of 5 A as shown. An electron is moving with a speed of $10^{5} \mathrm{~m} / \mathrm{s}$ parallel to the conductor. The perpendicular distance between the electron and the conductor is 20 cm at an instant. Calculate the magnitude of the force experienced by the electron at that instant.

(1) $4 \times 10^{-20} \mathrm{~N}$
(2) $8 \pi \times 10^{-20} \mathrm{~N}$
(3) $4 \pi \times 10^{-20} \mathrm{~N}$
(4) $8 \times 10^{-20} \mathrm{~N}$

## Ans. (4)

Sol.

$f=e v\left(\frac{\mu_{0} i}{2 \pi r}\right)$
$\mathrm{f}=\frac{1.6 \times 10^{-19} \times 10^{5} \times 2 \times 10^{-7} \times 5}{0.2}$
$\mathrm{f}=8 \times 10^{-20}$ Newton
17. If force [F], acceleration [A] and time [T] are chosen as the fundamental physical quantities. Find the dimensions of energy.
(1) $[\mathrm{F}][\mathrm{A}][\mathrm{T}]$
(2) $[\mathrm{F}][\mathrm{A}]\left[\mathrm{T}^{2}\right]$
(3) $[F][A]\left[\mathrm{T}^{-1}\right]$
(4) $[\mathrm{F}]\left[\mathrm{A}^{-1}\right][\mathrm{T}]$

## Ans. (2)

Sol. $E \propto F^{a} A^{b} T^{c}$
$\left[M^{1} L^{2} T^{-2}\right] \propto\left[M^{1} L^{1} T^{-2}\right]^{a}\left[L T^{-2}\right]^{b}[T]^{c}$
$a=1$
$\mathrm{a}+\mathrm{b}=2 \Rightarrow \mathrm{~b}=1$
$-2 a-2 b+c=-2$
$\Rightarrow c=2$

$$
a=1 \quad b=1 \quad c=2
$$

$\mathrm{E} \propto[\mathrm{F}][\mathrm{A}]\left[\mathrm{T}^{2}\right]$
18. Match Column-I and Column-II and choose the correct match from the given choices.

| Column-I |  | Column-II |  |
| :--- | :--- | :---: | :--- |
| (A) | Root mean square speed <br> of gas molecules | (P) | $\frac{1}{3} \mathrm{~nm}^{2}$ |
| (B) | Pressure exerted by ideal <br> gas | (Q) | $\sqrt{\frac{3 \mathrm{RT}}{\mathrm{M}}}$ |
| (C) | Average kinetic energy of <br> a molecule | (R) | $\frac{5}{2} \mathrm{RT}$ |
| (D) | Total internal energy of <br> 1 mole of a diatomic gas | (S) | $\frac{3}{2} \mathrm{k}_{\mathrm{B}} \mathrm{T}$ |

(1) (A) - (R), (B) - (P), (C) - (S), (D) - (Q)
(2) $(\mathrm{A})-(\mathrm{Q}),(\mathrm{B})-(\mathrm{R}),(\mathrm{C})-(\mathrm{S}),(\mathrm{D})-(\mathrm{P})$
(3) (A) - (Q), (B) - (P), (C) - (S), (D) - (R)
(4) (A) - (R), (B) - (Q), (C) - (P), (D) - (S)

Ans. (3)
Sol. Root mean sqaure speed of gas molecules

$$
v_{\mathrm{rms}}=\sqrt{\frac{3 \mathrm{RT}}{\mathrm{M}}}
$$

Pressure exerted by ideal Gas

$$
\begin{aligned}
& P=\frac{1}{3} \rho v_{\mathrm{rms}}^{2} \\
& P=\frac{1}{3} m n v^{2} \\
& \rho=\mathrm{mn}, v_{\mathrm{rms}}^{2}=\vec{v}^{2}
\end{aligned}
$$

Average kinetic energy of a molecular

$$
\mathrm{KE}=\frac{3}{2} \mathrm{KT}
$$

Total internal energy of 1 mole of a diatomic gas

$$
\mathrm{U}=\frac{\mathrm{f}}{2} \mu \mathrm{RT}
$$

$\mathrm{U}=\frac{5}{2} \mathrm{RT}$ (For 1 mole diatomic gas)

## Zin三du

19. A small block slides down on a smooth inclined plane, starting from rest at time $t=0$. Let $S_{n}$ be the distance travelled by the block in the interval $\mathrm{t}=\mathrm{n}-1$ to $\mathrm{t}=\mathrm{n}$. Then, the ratio $\frac{\mathrm{S}_{\mathrm{n}}}{\mathrm{S}_{\mathrm{n}+1}}$ is :
(1) $\frac{2 n-1}{2 n}$
(2) $\frac{2 n-1}{2 n+1}$
(3) $\frac{2 n+1}{2 n-1}$
(4) $\frac{2 n}{2 n-1}$

## Ans. (2)

Sol. $S_{n}=$ Distance in $n^{\text {th }}$ sec. i.e. $t=n-1$ to $t=n$ $S_{n+1}=$ Distance in $(n+1)^{\text {th }}$ sec.

$$
\text { i.e. } \mathrm{t}=\mathrm{n} \text { to } \mathrm{t}=\mathrm{n}+1
$$

So as we know

$$
\begin{aligned}
& \mathrm{S}_{\mathrm{n}}=\frac{a}{2}(2 \mathrm{n}-1) \quad a=\text { acceleration } \\
& \frac{\mathrm{S}_{\mathrm{n}}}{\mathrm{~S}_{\mathrm{n}+1}}=\frac{\frac{a}{2}(2 \mathrm{n}-1)}{\frac{\mathrm{a}}{2}(2(\mathrm{n}+1)-1)}=\frac{2 \mathrm{n}-1}{2 \mathrm{n}+1} \\
& \frac{\mathrm{~S}_{\mathrm{n}}}{\mathrm{~S}_{\mathrm{n}+1}}=\frac{2 \mathrm{n}-1}{2 \mathrm{n}+1}
\end{aligned}
$$

20. A nucleus with mass number 240 breaks into two fragments each of mass number 120, the binding energy per nucleon of unfragmented nuclei is 7.6 MeV while that of fragments is 8.5 MeV . The total gain in the Binding Energy in the process is :
(1) 0.9 MeV
(2) 9.4 MeV
(3) 804 MeV
(4) 216 MeV

## Ans. (4)

Sol. $X^{240} \rightarrow Y^{120}+Z^{120}$
given binding energy per nucleon of $\mathrm{X}, \mathrm{Y} \& \mathrm{Z}$ are 7.6 MeV, 8.5 MeV \& 8.5 MeV respectively.

Gain in binding energy is :-
$\mathrm{Q}=$ Binding Energy of products - Binding energy of reactants
$=(120 \times 8.5 \times 2)-(240 \times 7.6) \mathrm{MeV}$
$=216 \mathrm{MeV}$
21. A screw gauge gives the following readings when used to measure the diameter of a wire Main scale reading : 0 mm Circular scale reading : 52 divisions
Given that 1 mm on main scale corresponds to 100 divisions on the circular scale. The diameter of the wire from the above data is :
(1) 0.52 cm
(2) 0.026 cm
(3) 0.26 cm
(4) 0.052 cm

## Ans. (4)

Sol. Least count $=\frac{1 \mathrm{~mm}}{100}=0.01 \mathrm{~mm}$
$\begin{aligned} \text { Diameter }= & \text { main scale } \\ & \text { reading }\end{aligned}+\quad \begin{aligned} & \text { circular scale } \\ & \text { reading }\end{aligned}$
Diameter $=0+52 \times 0.01 \mathrm{~mm}$

$$
=0.52 \mathrm{~mm}=0.052 \mathrm{~cm}
$$

22. The equivalent capacitance of the combination shown in the figure is :

(1) 3 C
(2) 2 C
(3) $C / 2$
(4) $3 C / 2$

Ans. (2)

Sol.

(one capacitor gets short)

$$
\begin{aligned}
\Rightarrow C_{e q} & =C_{1}+C_{2} \\
& =C+C \\
& =2 C
\end{aligned}
$$

23. A lens of large focal length and large aperture is best suited as an objective of an astronomical telescope since :
(1) a large aperture contributes to the quality and visibility of the images.
(2) a large area of the objective ensures better light gathering power.
(3) a large aperture provides a better resolution.
(4) all of the above.

Ans. (4)

Sol. $\quad M P=\frac{\mathrm{f}_{0}}{\mathrm{f}_{e}}$
R.P. $=\frac{a}{1.22 \lambda}$
large aperture(a) of the objective lens provides better resolution $\therefore$ good quality of image is formed and also it gathers more light.
24. Two charged spherical conductors of radius $R_{1}$ and $\mathrm{R}_{2}$ are connected by a wire. Then the ratio of surface charge densities of the spheres $\left(\sigma_{1} / \sigma_{2}\right)$ is:
(1) $\frac{R_{1}}{R_{2}}$
(2) $\frac{R_{2}}{R_{1}}$
(3) $\sqrt{\left(\frac{\mathrm{R}_{1}}{\mathrm{R}_{2}}\right)}$
(4) $\frac{R_{1}^{2}}{R_{2}^{2}}$

Ans. (2)
Sol. For a conducting sphere
$E=\frac{\sigma}{\epsilon_{0}}$
$\mathrm{V}=\frac{\sigma \mathrm{R}}{\epsilon_{0}}$
as both spheres have same potential after connecting with wire,
$\mathrm{V}_{1}=\mathrm{V}_{2}$
$\sigma_{1} \mathrm{R}_{1}=\sigma_{2} \mathrm{R}_{2}$
$\Rightarrow \frac{\sigma_{1}}{\sigma_{2}}=\frac{\mathrm{R}_{2}}{\mathrm{R}_{1}}$
25. A spring is stretched by 5 cm by a force 10 N . The time period of the oscillations when a mass of 2 kg is suspended by it is :
(1) 0.0628 s
(2) 6.28 s
(3) 3.14 s
(4) 0.628 s

## Ans. (4)

Sol. $F=k x$
$10=\mathrm{k}\left(5 \times 10^{-2}\right)$
$\mathrm{k}=\frac{10}{5 \times 10^{-2}}=2 \times 10^{2}=200 \mathrm{~N} / \mathrm{m}$
Now $\mathrm{T}=2 \pi \sqrt{\frac{\mathrm{~m}}{\mathrm{k}}}=2 \pi \sqrt{\frac{2}{200}}=\frac{2 \pi}{10}=0.628 \mathrm{sec}$.
26. For a plane electromagnetic wave propagating in x -direction, which one of the following combination gives the correct possible directions for electric field $(\mathrm{E})$ and magnetic field $(\mathrm{B})$ respectively?
(1) $\hat{j}+\hat{k}, \hat{j}+\hat{k}$
(2) $-\hat{j}+\hat{k},-\hat{j}-\hat{k}$
(3) $\hat{j}+\hat{k},-\hat{j}-\hat{k}$
(4) $-\hat{j}+\hat{k},-\hat{j}+\hat{k}$

Ans. (2)
Sol. $\vec{v} \| \vec{E} \times \vec{B}, \hat{v}=\hat{i}$
Option (1) $\overrightarrow{\mathrm{E}} \times \overrightarrow{\mathrm{B}}=\overrightarrow{0} \quad(\overrightarrow{\mathrm{E}} \| \overrightarrow{\mathrm{B}})$
Option (2) $\overrightarrow{\mathrm{E}} \times \overrightarrow{\mathrm{B}}=2 \hat{\mathrm{i}}$ (parallel to $\overrightarrow{\mathrm{v}}$ )
Option (2) $\vec{E} \times \vec{B}=\overrightarrow{0}(\vec{E} \mid l \vec{B})$
Option (2) $\vec{E} \times \vec{B}=\overrightarrow{0} \quad(\vec{E} \| \vec{B})$
27. The escape velocity from the Earth's surface is $v$. The escape velocity from the surface of another planet having a radius, four times that of Earth and same mass density is:
(1) $v$
(2) $2 v$
(3) $3 v$
(4) $4 v$

Ans. (4)
Sol. $\quad v_{e}=\sqrt{\frac{2 G M}{\mathrm{R}}}=\sqrt{\frac{2 \mathrm{G}}{\mathrm{R}} \times \frac{4}{3} \pi \mathrm{R}^{3} \rho}$
$=\sqrt{\frac{8 \pi \mathrm{G} \rho}{3} \mathrm{R}^{2}}$
$\Rightarrow \mathrm{v}_{e} \propto \mathrm{R}$
$\Rightarrow \frac{\mathrm{v}_{e}}{\mathrm{v}}=\frac{4 \mathrm{R}}{\mathrm{R}} \Rightarrow \mathrm{v}_{e}=4 \mathrm{v}$
28. In a potentiometer circuit a cell of EMF 1.5 V gives balance point at 36 cm length of wire. If another cell of EMF 2.5 V replaces the first cell, then at what length of the wire, the balance point occurs?
(1) 60 cm
(2) 21.6 cm
(3) 64 cm
(4) 62 cm

Ans. (1)
Sol. $\frac{E_{1}}{E_{2}}=\frac{\phi \ell_{1}}{\phi \ell_{2}}$
$\frac{1.5}{2.5}=\frac{36}{\ell_{2}} \Rightarrow \ell_{2}=36 \times \frac{5}{3}=60 \mathrm{~cm}$
29. The velocity of a small ball of mass M and density d , when dropped in a container filled with glycerine becomes constant after some time. If the density of glycerine is $\frac{\mathrm{d}}{2}$, then the viscous force acting on the ball will be :
(1) $\frac{\mathrm{Mg}}{2}$
(2) Mg
(3) $\frac{3}{2} \mathrm{Mg}$
(4) 2 Mg

Ans. (1)
Sol. $\quad$ Mass $=M$


Density of ball $=\mathrm{d}$
Density of glycerine $=\frac{\mathrm{d}}{2}$
$\mathrm{F}_{\mathrm{B}}=\mathrm{V}_{\mathrm{s}} \rho_{\ell} \mathrm{g}=\mathrm{V} \frac{\mathrm{d}}{2} \mathrm{~g}$
$\mathrm{F}_{\mathrm{g}}=\mathrm{Mg}=\mathrm{vdg}$
for constant velocity, $\mathrm{F}_{\text {net }}=0$
$\therefore \quad \mathrm{F}_{\mathrm{B}}+\mathrm{F}_{\mathrm{v}}=\mathrm{M}_{\mathrm{g}}$

$$
\mathrm{F}_{\mathrm{v}}=\mathrm{M}_{\mathrm{g}}-\mathrm{F}_{\mathrm{B}}=\mathrm{Vdg}-\frac{\mathrm{Vdg}}{2}=\frac{\mathrm{Vdg}}{2}=\frac{\mathrm{Mg}}{2}
$$

30. A parallel plate capacitor has a uniform electric field ' $\vec{E}$ ' in the space between the plates. If the distance between the plates is 'd' and the area of each plate is ' A ', the energy stored in the capacitor is : ( $\varepsilon_{0}=$ permittivity of free space)
(1) $\frac{1}{2} \varepsilon_{0} E^{2}$
(2) $\varepsilon_{0} \mathrm{EAd}$
(3) $\frac{1}{2} \varepsilon_{0} \mathrm{E}^{2} \mathrm{Ad}$
(4) $\frac{E^{2} \mathrm{Ad}}{\varepsilon_{0}}$

Ans. (3)
Sol. $\mathrm{E}=\frac{1}{2} \mathrm{CV}^{2}$

$$
\begin{aligned}
& =\frac{1}{2}\left(\frac{\varepsilon_{0} \mathrm{~A}}{\mathrm{~d}}\right)(\mathrm{Ed})^{2} \\
& =\frac{1}{2} \varepsilon_{0} \mathrm{E}^{2} \mathrm{Ad}
\end{aligned}
$$

31. The electron concentration in an $n$-type semiconductor is the same as hole concentration in a p-type semiconductor. An external field (electric) is applied across each of them. Compare the currents in them.
(1) current in n-type $=$ current in p-type
(2) current in p-type > current in n-type
(3) current in n-type > current in p-type
(4) No current will flow in p-type, current will only flow in n-type
Ans. (3)
Sol. In N type semiconductor majority charge carriers are $e^{-}$and P type semiconductor majority charge carriers are holes.
$\mathrm{I}=\mathrm{neAV} \mathrm{D}_{\mathrm{d}}=\mathrm{neA}(\mu \mathrm{E})$
$\mu_{e}>\mu_{\mathrm{h}} \Rightarrow \mathrm{I}_{e}>\mathrm{I}_{\mathrm{h}}$
32. Consider the following statements (A) and (B) and identify the correct answer.
(A) A zener diode is connected in reverse bias, when used as a voltage regulator.
(B) The potential barrier of $\mathrm{p}-\mathrm{n}$ junction lies between 0.1 V to 0.3 V .
(1) $\mathbf{( A )}$ and (B) both are correct.
(2) (A) and (B) both are incorrect.
(3) $\mathbf{( A )}$ is correct and $(\mathbf{B})$ is incorrect.
(4) $(\mathbf{A})$ is incorrect but $(B)$ is correct.

Ans. (3)
Sol. Reverse bias Zener diode use as a voltage regulator
for Ge Potential barrier $\mathrm{V}_{0}=0.3 \mathrm{~V}$
Si Potential barrier $\mathrm{V}_{0}=0.7 \mathrm{~V}$
33. Polar molecules are the molecules :
(1) having zero dipole moment.
(2) acquire a dipole moment only in the presence of electric field due to displacement of charges.
(3) acquire a dipole moment only when magnetic field is absent.
(4) having a permanent electric dipole moment.

## Ans. (4)

Sol. Polar molecules have centres of postive and negative charges separated by some distance, so they have permanent dipole moment.
34. If $E$ and $G$ respectively denote energy and gravitational constant, then $\frac{E}{G}$ has the dimensions of :
(1) $\left[\mathrm{M}^{2}\right]\left[\mathrm{L}^{-1}\right]\left[\mathrm{T}^{0}\right]$
(2) $[\mathrm{M}]\left[\mathrm{L}^{-1}\right]\left[\mathrm{T}^{-1}\right]$
(3) $[\mathrm{M}]\left[\mathrm{L}^{0}\right]\left[\mathrm{T}^{0}\right]$
(4) $\left[\mathrm{M}^{2}\right]\left[\mathrm{L}^{-2}\right]\left[\mathrm{T}^{-1}\right]$

Ans. (1)
Sol. $E=$ energy $=\left[M L^{2} T^{-2}\right]$
$\mathrm{G}=$ Gravitational constant $=\left[\mathrm{M}^{-1} \mathrm{~L}^{3} \mathrm{~T}^{-2}\right]$
So $\frac{E}{G}=\frac{[E]}{[G]}=\frac{M L^{2} \mathrm{~T}^{-2}}{\mathrm{M}^{-1} \mathrm{~L}^{3} \mathrm{~T}^{-2}}=\left[\mathrm{M}^{2} \mathrm{~L}^{-1} \mathrm{~T}^{0}\right]$
35. Water falls from a height of 60 m at the rate of $15 \mathrm{~kg} / \mathrm{s}$ to operate a turbine. The losses due to frictional force are $10 \%$ of the input energy. How much power is generated by the turbine?
$\left(\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}\right)$
(1) 10.2 kW
(2) 8.1 kW
(3) 12.3 kW
(4) 7.0 kW

Ans. (2)
Sol. $P_{i n}=\frac{\mathrm{mgh}}{\mathrm{t}}=\frac{15 \times 10 \times 60}{1}$
$=9000 \mathrm{w}$
$\mathrm{P}_{\text {out }}=90 \%$ of $\mathrm{P}_{\text {in }}$
$\Rightarrow 8.1 \mathrm{kw}$

## SECTION-B

36. A car starts from rest and accelerates at $5 \mathrm{~m} / \mathrm{s}^{2}$. At $t=4 \mathrm{~s}$, a ball is dropped out of a window by a person sitting in the car. What is the velocity and acceleration of the ball at $t=6 \mathrm{~s}$ ?
(Take $\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$ )
(1) $20 \mathrm{~m} / \mathrm{s}, 5 \mathrm{~m} / \mathrm{s}^{2}$
(2) $20 \mathrm{~m} / \mathrm{s}, 0$
(3) $20 \sqrt{2} \mathrm{~m} / \mathrm{s}, 0$
(4) $20 \sqrt{2} \mathrm{~m} / \mathrm{s}, 10 \mathrm{~m} / \mathrm{s}^{2}$

## Ans. (4)

Sol. velocity of car at $t=4 \mathrm{sec}$ is

$$
\begin{aligned}
\mathrm{v} & =\mathrm{u}+\mathrm{at} \\
\mathrm{v} & =0+5(4) \\
& =20 \mathrm{~m} / \mathrm{s}
\end{aligned}
$$

At $\mathrm{t}=6 \mathrm{sec}$
acceleration is due to gravity $\therefore \mathrm{a}=\mathrm{g}=10 \mathrm{~m} / \mathrm{s}$

$$
\begin{aligned}
\mathrm{v}_{\mathrm{x}} & =20 \mathrm{~m} / \mathrm{s} \text { (due to car) } \\
\mathrm{v}_{\mathrm{y}} & =\mathrm{u}+\mathrm{at} \\
& =0+\mathrm{g}(2) \text { (downward) } \\
& =20 \mathrm{~m} / \mathrm{s} \text { (downward) } \\
\mathrm{v} & =\sqrt{\mathrm{v}_{\mathrm{x}}^{2}+\mathrm{v}_{\mathrm{y}}^{2}} \\
& =\sqrt{20^{2}+20^{2}} \\
& =20 \sqrt{2} \mathrm{~m} / \mathrm{s}
\end{aligned}
$$

37. For the given circuit, the input digital signals are applied at the terminals A, B and C. What would be the output at the terminal $y$ ?


A

(1)

(2)

(3)


Ans. (3)
Sol. $\mathrm{Y}=\mathrm{A} \cdot \mathrm{B}+\overline{\mathrm{B} \cdot \mathrm{C}}$
(i) 0 to $t_{1} \quad \mathrm{~A}=0, \mathrm{~B}=0, \mathrm{C}=1$

$$
Y=0 \cdot 0+\overline{0 \cdot 1}=0+1=1
$$

39. A uniform rod of length 200 cm and mass 500 g is balanced on a wedge placed at 40 cm mark. A mass of 2 kg is suspended from the rod at 20 cm and another unknown mass ' $m$ ' is suspended from the rod at 160 cm mark as shown in the figure. Find the value of ' m ' such that the rod is in equilibrium. $\left(\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}\right)$

(1) $\frac{1}{2} \mathrm{~kg}$
(2) $\frac{1}{3} \mathrm{~kg}$
(3) $\frac{1}{6} \mathrm{~kg}$
(4) $\frac{1}{12} \mathrm{~kg}$

Ans. (4)

Sol.


By balancing torque
$2 \mathrm{~g} \times 20=0.5 \mathrm{~g} \times 60+\mathrm{mg} \times 120$
$\mathrm{m}=\frac{0.5}{6} \mathrm{~kg}=\frac{1}{12} \mathrm{~kg}$
40. A point object is placed at a distance of 60 cm from a convex lens of focal length 30 cm . If a plane mirror were put perpendicular to the principal axis of the lens and at a distance of 40 cm from it, the final image would be formed at a distance of :

(1) 20 cm from the lens, it would be a real image.
(2) 30 cm from the lens, it would be a real image.
(3) 30 cm from the plane mirror, it would be a virtual image.
(4) 20 cm from the plane mirror, it would be a virtual image.
Ans. (4)

Sol. first, for image formation from lens
$u=-60 \mathrm{~cm}$
$\mathrm{f}=+30 \mathrm{~cm}$
$\Rightarrow \mathrm{v}=\frac{\mathrm{uf}}{\mathrm{u}+\mathrm{f}}=\frac{-60 \times 30}{-60+30}=60 \mathrm{~cm}$
this real image formed by lens acts as virtual object for mirror


Real image from plane mirror is formed 20 cm in front of mirror, hence at 20 cm distance from lens. Now, for second refraction from lens,
$\mathrm{u}=-20 \mathrm{~cm}$
$\mathrm{f}=+30 \mathrm{~cm}$
$v=\frac{u f}{u+f}=\frac{-20 \times 30}{-20+30}=-60 \mathrm{~cm}$
So, final virtual image is 60 cm from lens, or 20 cm behind mirror

41. A step down transformer connected to an ac mains supply of 220 V is made to operate at $11 \mathrm{~V}, 44 \mathrm{~W}$ lamp. Ignoring power losses in the transformer, what is the current in the primary circuit?
(1) 0.2 A
(2) 0.4 A
(3) 2 A
(4) 4 A

## Ans. (1)

Sol. $220 \times i_{p}=44$
$\Rightarrow \mathrm{i}_{\mathrm{p}}=\frac{44}{220}=\frac{1}{5}=0.2 \mathrm{~A}$
42. Three resistors having resistances $r_{1}, r_{2}$ and $r_{3}$ are connected as shown in the given circuit. The ratio $\frac{i_{3}}{i_{1}}$ of currents in terms of resistances used in the circuit is :

(1) $\frac{r_{1}}{r_{2}+r_{3}}$
(2) $\frac{r_{2}}{r_{2}+r_{3}}$
(3) $\frac{r_{1}}{r_{1}+r_{2}}$
(4) $\frac{r_{2}}{r_{1}+r_{3}}$

Ans. (2)
Sol. $\mathrm{V}=\mathrm{ir}$
$i=\frac{V}{r}$
$i \propto \frac{1}{r}\left[v\right.$ is same for $\left.r_{2} \& r_{3}\right]$
$\frac{i_{2}}{i_{3}}=\frac{r_{3}}{r_{2}}$
$\mathrm{i}_{3}=\frac{\mathrm{r}_{2}}{\mathrm{r}_{2}+\mathrm{r}_{3}} \mathrm{i}_{1}$

$\frac{\mathrm{i}_{3}}{\mathrm{i}_{1}}=\frac{\mathrm{r}_{2}}{\mathrm{r}_{2}+\mathrm{r}_{3}}$
43. In the product

$$
\begin{aligned}
\overrightarrow{\mathrm{F}} & =q(\overrightarrow{\mathrm{v}} \times \overrightarrow{\mathrm{B}}) \\
& =q \overrightarrow{\mathrm{v}} \times\left(B \hat{i}+B \hat{j}+B_{0} \hat{k}\right)
\end{aligned}
$$

For $q=1$ and $\vec{v}=2 \hat{i}+4 \hat{j}+6 \hat{k}$ and

$$
\overrightarrow{\mathrm{F}}=4 \hat{\mathrm{i}}-20 \hat{\mathrm{j}}+12 \hat{k}
$$

What will be the complete expression for $\vec{B}$ ?
(1) $-8 \hat{\mathbf{i}}-8 \hat{\mathbf{j}}-6 \hat{\mathbf{k}}$
(2) $-6 \hat{\mathbf{i}}-6 \hat{\mathbf{j}}-8 \hat{\mathbf{k}}$
(3) $8 \hat{\mathrm{i}}+8 \hat{\mathrm{j}}-6 \hat{\mathrm{k}}$
(4) $6 \hat{i}+6 \hat{j}-8 \hat{k}$

Ans. (2)

Sol. $\quad \vec{F}=q(\vec{v} \times \vec{B})$
$4 i-20 j+12 \hat{k}=1\left|\begin{array}{ccc}i & j & \hat{k} \\ 2 & 4 & 6 \\ B & B & B_{0}\end{array}\right|$
Comparing
$\left.\begin{array}{c}\Rightarrow 4=4 \mathrm{~B}_{0}-6 \mathrm{~B} \\ -20=-2 \mathrm{~B}_{0}+6 \mathrm{~B} \\ 12=2 \mathrm{~B}-4 \mathrm{~B}\end{array}\right\} \begin{gathered}\text { Solving } \\ \mathrm{B}=-6 \\ \mathrm{~B}_{0}=-8\end{gathered}$
$\therefore \quad \vec{B}=-6 \hat{i}-6 \hat{j}-8 \hat{k}$
44. A particle of mass ' $m$ ' is projected with a velocity $\mathrm{v}=\mathrm{kV} \mathrm{V}_{e}(\mathrm{k}<1)$ from the surface of the earth.
( $\mathrm{V}_{e}=$ escape velocity)
The maximum height above the surface reached by the particle is :
(1) $\mathrm{R}\left(\frac{\mathrm{k}}{1-\mathrm{k}}\right)^{2}$
(2) $\mathrm{R}\left(\frac{\mathrm{k}}{1+\mathrm{k}}\right)^{2}$
(3) $\frac{\mathrm{R}^{2} \mathrm{k}}{1+\mathrm{k}}$
(4) $\frac{\mathrm{Rk}^{2}}{1-\mathrm{k}^{2}}$

Ans. (4)
Sol. $\mathrm{h}=\frac{\mathrm{R}}{\frac{2 \mathrm{~g} \mathrm{R}}{\mathrm{V}^{2}}-1}=\frac{\mathrm{R}}{\frac{\mathrm{V}_{e}^{2}}{\mathrm{~K}^{2} \mathrm{~V}_{e}^{2}}-1}=\frac{\mathrm{RK}^{2}}{1-\mathrm{K}^{2}}$
45. Twenty seven drops of same size are charged at 220 V each. They combine to form a bigger drop. Calculate the potential of the bigger drop.
(1) 660 V
(2) 1320 V
(3) 1520 V
(4) 1980 V

## Ans. (4)

Sol. $\quad \frac{4}{3} \pi R^{3}=27\left(\frac{4}{3} \pi r^{3}\right) \Rightarrow R=3 r$
$\mathrm{V}=\frac{\mathrm{Kq}}{\mathrm{r}} \Rightarrow \frac{\mathrm{V}_{1}}{\mathrm{~V}_{2}}=\left(\frac{\mathrm{q}_{1}}{\mathrm{q}_{2}}\right)\left(\frac{\mathrm{r}_{2}}{\mathrm{r}_{1}}\right)$
$\Rightarrow \frac{220}{\mathrm{~V}_{2}}=\left(\frac{\mathrm{q}}{27 \mathrm{q}}\right)\left(\frac{3 \mathrm{r}}{\mathrm{r}}\right)$
$\Rightarrow \frac{220}{\mathrm{~V}_{2}}=\frac{1}{9}$
$\Rightarrow V_{2}=220 \times 9=1980$ Volt
46. A series LCR circuit containing 5.0 H inductor, $80 \mu \mathrm{~F}$ capacitor and $40 \Omega$ resistor is connected to 230 V variable frequency ac source. The angular frequencies of the source at which power transferred to the circuit is half the power at the resonant angular frequency are likely to be :
(1) $25 \mathrm{rad} / \mathrm{s}$ and $75 \mathrm{rad} / \mathrm{s}$
(2) $50 \mathrm{rad} / \mathrm{s}$ and $25 \mathrm{rad} / \mathrm{s}$
(3) $46 \mathrm{rad} / \mathrm{s}$ and $54 \mathrm{rad} / \mathrm{s}$
(4) $42 \mathrm{rad} / \mathrm{s}$ and $58 \mathrm{rad} / \mathrm{s}$

## Ans. (3)

Sol. $\mathrm{Q}=\frac{\omega}{\Delta \omega}=\frac{\omega \mathrm{L}}{\mathrm{R}} \Rightarrow \Delta \omega=\mathrm{R} / \mathrm{L}=\frac{50}{4}=8 \mathrm{rad} / \mathrm{sec}$
$\omega_{0}=\frac{1}{\sqrt{\mathrm{LC}}}=\frac{1}{\sqrt{5 \times 80 \times 10^{-6}}}=50 \mathrm{rad} / \mathrm{sec}$.
$\omega_{\text {min }}=\omega_{0}-\frac{\Delta \omega}{2}=46 \mathrm{rad} / \mathrm{sec}$
$\omega_{\text {max }}=\omega_{0}-\frac{\Delta \omega}{2}=54 \mathrm{rad} / \mathrm{sec}$
47. A uniform conducting wire of length 12a and resistance ' R ' is wound up as a current carrying coil in the shape of,
(i) an equilateral triangle of side 'a'.
(ii) a square of side 'a'.

The magnetic dipole moments of the coil in each case respectively are:
(1) $\sqrt{3} \mathrm{Ia}^{2}$ and $3 \mathrm{Ia}^{2}$
(2) $3 \mathrm{Ia}^{2}$ and $\mathrm{Ia}^{2}$
(3) $3 \mathrm{Ia}^{2}$ and $4 \mathrm{Ia}^{2}$
(4) $4 \mathrm{Ia}^{2}$ and $3 \mathrm{Ia}^{2}$

## Ans. (1)

Sol. $\quad M_{1}=\left(\frac{\sqrt{3}}{4} a^{2}\right) I \times 4=\sqrt{3} \mathrm{Ia}^{2}($ no. of turns $=4)$
$\mathrm{M}_{2}=\mathrm{a}^{2} \mathrm{I} \times 3=3 \mathrm{Ia}^{2}($ no. of turns $=3)$
48. From a circular ring of mass ' $M$ ' and radius ' $R$ ' an arc corresponding to a $90^{\circ}$ sector is removed. The moment of inertia of the remaining part of the ring about an axis passing through the centre of the ring and perpendicular to the plane of the ring is ' K ' times ' $\mathrm{MR}^{2}$ '. Then the value of ' K ' is :
(1) $\frac{3}{4}$
(2) $\frac{7}{8}$
(3) $\frac{1}{4}$
(4) $\frac{1}{8}$

Ans. (1)
Sol. $\quad M_{\text {remain }}=\frac{3}{4} M$

$$
\begin{aligned}
\mathrm{I} & =\mathrm{M}_{\mathrm{remain}} \mathrm{R}^{2} \\
& =\frac{3}{4} \mathrm{MR}^{2}
\end{aligned}
$$


49. Two conducting circular loops of radii $R_{1}$ and $R_{2}$ are placed in the same plane with their centres coinciding. If $R_{1} \gg R_{2}$, the mutual inductance $M$ between them will be directly proportional to:
(1) $\frac{R_{1}}{R_{2}}$
(2) $\frac{R_{2}}{R_{1}}$
(3) $\frac{R_{1}^{2}}{R_{2}}$
(4) $\frac{R_{2}^{2}}{R_{1}}$

Ans. (4)
Sol. $\mathrm{M}=\frac{\phi_{12}}{\mathrm{I}_{1}}=\frac{\mathrm{B}_{1} \mathrm{~A}_{2}}{\mathrm{I}_{1}}=\frac{\left(\frac{\mu_{0} \mathrm{I}_{1}}{2 \mathrm{R}_{1}}\right)\left(\pi \mathrm{R}_{2}^{2}\right)}{\mathrm{I}_{1}}$

$$
\mathrm{M}=\frac{\mu_{0} \pi \mathrm{R}_{2}^{2}}{2 \mathrm{R}_{1}}
$$

$M \propto \frac{R_{2}^{2}}{R_{1}}$
50. A particle moving in a circle of radius R with a uniform speed takes a time T to complete one revolution.
If this particle were projected with the same speed at an angle ' $\theta$ ' to the horizontal, the maximum height attained by it equals 4R. The angle of projection, $\theta$, is then given by :
(1) $\theta=\cos ^{-1}\left(\frac{g T^{2}}{\pi^{2} R}\right)^{1 / 2}$
(2) $\theta=\cos ^{-1}\left(\frac{\pi^{2} R}{g T^{2}}\right)^{1 / 2}$
(3) $\theta=\sin ^{-1}\left(\frac{\pi^{2} \mathrm{R}}{\mathrm{gT}^{2}}\right)^{1 / 2}$
(4) $\theta=\sin ^{-1}\left(\frac{2 g T^{2}}{\pi^{2} \mathrm{R}}\right)^{1 / 2}$

Ans. (4)
Sol. $T=\frac{2 \pi R}{v} \Rightarrow v=\frac{2 \pi R}{T}$
$H_{\max }=\frac{v^{2} \sin ^{2} \theta}{2 g}=\frac{2 \pi^{2} R^{2} \sin ^{2} \theta}{g T^{2}}=4 R$
$\sin \theta=\left(\frac{2 g T^{2}}{\pi^{2} \mathrm{R}}\right)^{1 / 2}$
$\theta=\sin ^{-1}\left[\frac{2 \mathrm{~g} \mathrm{~T}^{2}}{\pi^{2} \mathrm{R}}\right]^{1 / 2}$

